

Phy 523  
PARTICLE PHYSICS

12th January 2009

Due 19th January 2009

1. Consider a particle A ( mass  $M_A$ ) decaying to two particles B,C ( masses  $M_B, M_C$ ). Find the momentum of particle B in the (a) rest frame of A and (b) in a frame in which the momentum of A is  $\vec{P}_A = (0, 0, P_A)$  and the momentum of B makes an angle  $\theta$  with A.

2. Consider a particle A ( mass  $M_A$ ) decay to three particles B,C and D ( masses  $M_B, M_C$  and  $M_D$ ). Find the maximum and the minimum energy range for C in the rest frame of A.

3. Consider the scattering  $A+B \rightarrow C+D$ . Masses are  $(M_A, M_B, M_C, M_D)$  respectively with  $M_C + M_D > M_A + M_D$ . Find the minimum energy needed for the particle A in order this reaction occurs (a) in the rest frame of B (b) in the centre of mass frame.

4. Consider the decay  $\pi^0 \rightarrow \gamma + \gamma$  ( mass of pion is  $M_\pi$ ). Assume that the decay is isotropic in the rest frame of  $\pi^0$ . Now consider a frame  $\pi^0$  is moving with energy  $E$ . Show that the energy distribution of the photons in this frame is given by

$$\frac{dN(E_\gamma)}{dE_\gamma} = \text{constant}$$

where  $N(E_\gamma)$  is the number of photons emitted as a function of the energy of the photon  $E_\gamma$ . Further show that  $E(1 - \beta) < E_\gamma < E(1 + \beta)$  where  $\beta = (E^2 - M_\pi^2)^{1/2}/E$

5.(a) The life time of a particle in natural units (  $\hbar = c = 1$ ) is  $1\text{Mev}^{-1}$ . Find the lifetime in seconds.

(b) the cross section of scattering in a process is  $1\text{Mev}^{-2}$ . Find the cross section in  $\text{cm}^2$ .