

Phy 523
PARTICLE PHYSICS
Problem sheet IV

3rd February 2009

February 10th 2009

16. Relate the matrix elements of the decay $\Delta^{++}, \Delta^+, \Delta^0$ and Δ^- to pions and nucleons assuming isospin invariance. ($I(\Delta) = 3/2$).

17. Generalised statistics states that isospin wave function \times spin wave function \times spatial wave function should be symmetric (antisymmetric) for bosons (fermions). Find the combinations allowed (isospin, spin and spatial) for (a) two pions (b) two nucleons.

18. Isospin (J^P) of ω^0 is $I=1$ and 1^- . (Its mass is $780 \text{ MeV}/c^2$) Show that it can not decay into two pions if isospin is conserved. Given that deuteron is in $l=0, S=1$ find the isospin of deuteron.

19. η^0 is an $I=0$ and $J^P = 0^-$ particle. (Its mass $= 550 \text{ MeV}/c^2$) Show that it can not decay to two pions if parity is conserved in the decay.

20. ω^0 decays to three pions, $\omega^0 \rightarrow \pi^0 + \pi^+ + \pi^-$. Let the average energies of π^+, π^- be $\langle E_+ \rangle, \langle E_- \rangle$ respectively. (a) Write down an expression for the average values $\langle E_+ \rangle$ and $\langle E_- \rangle$ in terms of $|M|^2$ and phase space integral over the three momenta of pions. ($|M|^2$ is the square of the appropriate matrix element.) (b) Show that if C or CP is conserved in the decay $\langle E_+ \rangle = \langle E_- \rangle$.