

A particle of mass m moves in a two dimensional potential $V(x, y) = \frac{1}{2}(4x^2 + y^2)$ and is in an energy eigen state. Following four different un-normalized wave functions are given

(a) $\psi_1(x) = y \exp\left(-\frac{m\omega}{\hbar}(2x^2 + y^2)\right)$

(b) $\psi_1(x) = xy \exp\left(-\frac{m\omega}{\hbar}(2x^2 + y^2)\right)$

(c) $\psi_1(x) = x \exp\left(-\frac{m\omega}{\hbar}(x^2 + y^2)\right)$

(d) $\psi_1(x) = y \exp\left(-\frac{m\omega}{\hbar}(2x^2 + y^2)\right)$

(e) $\psi_1(x) = \exp\left(-\frac{m\omega}{\hbar}(x^2 + 2y^2)\right)$

(f) $\psi_1(x) = y \exp\left(-\frac{m\omega}{\hbar}(2x^2 + y^2)\right)$

For each of the above functions find if it is the eigen function of the energy, and [2]if it is, find the corresponding energy.