CHENNAI MATHEMATICAL INSTITUTE CLASSICAL MECHANICS I PROBLEM SHEET IV

 $3rd \ September \ 2012 \\ date \ due \ 10th \ September \ 2012$

- 16. Consider an undamped simple harmonic oscillator and trace the trajectory of a point A with initial conditions x(t=0) = A; p(t=0) = 0 in phase space. Choose three neighbouring points in phase space and show that the area of the triangle in phase space is independent of time.
- 17. Consider the motion of a particle of mass M whose motion is given by

$$M\frac{d^2z}{dt^2} + \lambda \frac{dz}{dt} = mg$$

Choose an appropriate initial condition for the motion of the particle and trace it's trajectory in phase space. Choosing three neighbouring points at time t=0 and find the area of the triangle in phase space and show it is not independent of time.

18.Draw the phase space plot of a few trajectories for a particle moving under the potential

$$V(x) = -ax + bx^3 a, b > 0$$

You need not solve the equation of motion. Draw the potential and use physical arguments to get the trajectories for different initial conditions. When will the trajectory be closed?

- 19. Consider the motion of a particle described by $\vec{r}(t)$. Find the velocity and acceleration vectors in spherical polar coordinates (r, θ, ϕ) along $(\hat{r}, \hat{\theta}, \hat{\phi})$.
- 20. A pendulum has a period of one second in vacuum. When placed in a resistive medium (resistance is proportional to the velocity), it is observed that the amplitude on each swing becomes half that of the previous swing. What is it's new period?